

宇田方程式

原型

$$\frac{i\hbar}{\alpha} \lim_{\varepsilon \rightarrow 0} \frac{\Phi[\chi(\square - \varepsilon)] - \Phi[\chi]}{\varepsilon}$$

$$= \int_{-\infty}^{\infty} dt \left\{ \frac{1}{2m} \left[-\frac{i\hbar}{\alpha} \cdot \frac{\delta}{\delta\chi(t)} \right]^2 + V(\chi(t)) \right\} \Phi[\chi]$$

変型

$$\left\{ \frac{1}{2m} \int_{-\infty}^{\infty} dt \left[-\frac{i\hbar}{\alpha} \cdot \frac{\delta}{\delta\chi(t)} - m \frac{d\chi(t)}{dt} \right]^2 - S[\chi] \right\} \Phi[\chi] = 0$$

$$S[\chi] \equiv \int_{-\infty}^{\infty} dt \left\{ \frac{m}{2} \left[\frac{d\chi(t)}{dt} \right]^2 - V(\chi(t)) \right\}$$

$V=0$ の場合

$$\int_{-\infty}^{\infty} dt \left\{ \frac{1}{2m} \left[-\frac{i\hbar}{\alpha} \cdot \frac{\delta}{\delta\chi(t)} - m \frac{d\chi(t)}{dt} \right]^2 - \frac{m}{2} \left[\frac{d\chi(t)}{dt} \right]^2 \right\} \Phi[\chi] = 0$$

$$\int_{-\infty}^{\infty} dt \left\{ \frac{1}{2m} \left[-\frac{i\hbar}{\alpha} \cdot \frac{\delta}{\delta\chi(t)} \right]^2 + \frac{i\hbar}{\alpha} \cdot \frac{d\chi(t)}{dt} \cdot \frac{\delta}{\delta\chi(t)} \right\} \Phi[\chi] = 0$$