

$$u_{e_1}(x) = \sum_{n=0}^{\infty} a_{2n+1} x^{2n+1}$$

$$u_{e_2}(x) = \sum_{n=0}^{\infty} a_{2n} x^{2n}$$

$$x u_{e_1}(x) = \int de' \xi_1(e, e') u_{e'_2}(x)$$

$$x u_{e_2}(x) = \int de' \xi_2(e, e') u_{e'_1}(x)$$

$$-i\hbar \frac{d}{dx} u_{e_1}(x) = \int de' \eta_1(e, e') u_{e'_2}(x)$$

$$-i\hbar \frac{d}{dx} u_{e_2}(x) = \int de' \eta_2(e, e') u_{e'_1}(x)$$

$$\xi_1(e, e') = \frac{a_1(e)}{a_2(e')} \cdot \frac{\Gamma\left(\frac{5}{4} + \frac{e'}{4i\hbar m \alpha}\right)}{\Gamma\left(\frac{3}{4} + \frac{e}{4i\hbar m \alpha}\right)} \left[ \delta(e + 2i\hbar m \alpha - e') + \left(\frac{1}{4} - \frac{e}{4i\hbar m \alpha}\right) \delta(e - 2i\hbar m \alpha - e') \right]$$

$$\xi_2(e, e') = \frac{-\hbar}{im \alpha} \cdot \frac{a_2(e)}{a_1(e')} \cdot \frac{\Gamma\left(\frac{3}{4} + \frac{e'}{4i\hbar m \alpha}\right)}{\Gamma\left(\frac{5}{4} + \frac{e}{4i\hbar m \alpha}\right)} \left[ \delta(e + 2i\hbar m \alpha - e') + \left(\frac{1}{4} - \frac{e}{4i\hbar m \alpha}\right) \delta(e - 2i\hbar m \alpha - e') \right]$$

$$\eta_1(e, e') = -2m \alpha \frac{a_1(e)}{a_2(e')} \cdot \frac{\Gamma\left(\frac{5}{4} + \frac{e'}{4i\hbar m \alpha}\right)}{\Gamma\left(\frac{3}{4} + \frac{e}{4i\hbar m \alpha}\right)} \delta(e + 2i\hbar m \alpha - e')$$

$$\eta_2(e, e') = -2i\hbar \frac{a_2(e)}{a_1(e')} \cdot \frac{\Gamma\left(\frac{3}{4} + \frac{e'}{4i\hbar m \alpha}\right)}{\Gamma\left(\frac{5}{4} + \frac{e}{4i\hbar m \alpha}\right)} \delta(e + 2i\hbar m \alpha - e')$$