

$n=3$ の場合を考える事によって、

$$\varepsilon = \frac{1}{3}$$

$$\sum_{k=1}^3 \varepsilon \left\{ \frac{1}{2m} \left[ -\frac{i\pi}{\alpha} \frac{1}{\varepsilon} \frac{\partial}{\partial \chi(k\varepsilon)} - m \frac{\chi(k\varepsilon+\varepsilon) - \chi(k\varepsilon)}{\varepsilon} \right]^2 - \frac{m}{2} \left[ \frac{\chi(k\varepsilon+\varepsilon) - \chi(k\varepsilon)}{\varepsilon} \right]^2 \right\} \Phi(\chi(\varepsilon), \chi(2\varepsilon), \chi(3\varepsilon)) = 0$$


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$$\begin{aligned} & \sum_{k=1}^3 \varepsilon \left\{ \frac{1}{2m} \left[ -\frac{i\pi}{\alpha} \frac{1}{\varepsilon} \frac{\partial}{\partial \chi(k\varepsilon)} - m \frac{\chi(k\varepsilon+\varepsilon) - \chi(k\varepsilon)}{\varepsilon} \right]^2 - \frac{m}{2} \left[ \frac{\chi(k\varepsilon+\varepsilon) - \chi(k\varepsilon)}{\varepsilon} \right]^2 \right\} \\ &= \varepsilon \frac{1}{2m} \left[ -\frac{i\pi}{\alpha} \frac{1}{\varepsilon} \frac{\partial}{\partial \chi(\varepsilon)} - m \frac{\chi(2\varepsilon) - \chi(\varepsilon)}{\varepsilon} \right]^2 - \varepsilon \frac{m}{2} \left[ \frac{\chi(2\varepsilon) - \chi(\varepsilon)}{\varepsilon} \right]^2 \\ &+ \varepsilon \frac{1}{2m} \left[ -\frac{i\pi}{\alpha} \frac{1}{\varepsilon} \frac{\partial}{\partial \chi(2\varepsilon)} - m \frac{\chi(3\varepsilon) - \chi(2\varepsilon)}{\varepsilon} \right]^2 - \varepsilon \frac{m}{2} \left[ \frac{\chi(3\varepsilon) - \chi(2\varepsilon)}{\varepsilon} \right]^2 \\ &+ \varepsilon \frac{1}{2m} \left[ -\frac{i\pi}{\alpha} \frac{1}{\varepsilon} \frac{\partial}{\partial \chi(3\varepsilon)} - m \frac{\chi(4\varepsilon) - \chi(3\varepsilon)}{\varepsilon} \right]^2 - \varepsilon \frac{m}{2} \left[ \frac{\chi(4\varepsilon) - \chi(3\varepsilon)}{\varepsilon} \right]^2 \end{aligned}$$

$$\chi(4\varepsilon) = \chi(\varepsilon)$$